1 Electron extraction mechanisms of a micro-ECR neutralizer

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13	Abstract
14	Three-dimensional particle simulations have been conducted to analyze the mechanisms of
15	electron extraction through the orifices of a 4.2 GHz microwave discharge microneutralizer,
16	using a xenon electron cyclotron resonance plasma. The dimensions of the neutralizer are

17 $20 \times 20 \times 4 \text{ mm}^3$, and a ring-shaped microwave antenna and permanent magnets are employed for

18 its discharges. The numerical model is composed of a particle-in-cell simulation with a Monte

- 19 Carlo collision algorithm for charged particle motions, a finite-difference time-domain method
- 20 for microwaves, and a finite element analysis for magnetostatic fields. The simulation results

have shown that the electrostatic field inside the plasma source has a dominant effect on electron extraction. The extracted electrons move along the magnetic field line to the orifice entrances and the $E \times B$ drift at the orifice edge induces electron extraction.

25 **1. Introduction**

Electron sources are widely used in various fields from basic sciences to industrial applications, 26 such as γ -ray sources,¹⁾ high-current electron beams for microwave tubes,²⁾ inductively coupled 27 plasma mass spectrometry,³⁾ etching tools,⁴⁾ welding flow lines,⁵⁾ and neutralization of ion 28 beams for ion and Hall thrusters.⁶⁾ Neutralization is required for not only ion and Hall thrusters 29 30 but also a low-energy ion implantation along with shrinkage of transistors to cancel out the space charge effect for shallow depths of implants.⁷⁾ Most electron sources are generated by 31 plasma discharges, and a micro-electron source, a neutralizer which we report here, also 32 employs a plasma discharge sustained by electron cyclotron resonance (ECR). 33 The micro-ECR neutralizer presented here was developed by the University of Tokyo, 34

and it is one of the components of a miniature ion propulsion system (MIPS) for a 50-kg-class microspacecraft, HODOYOSHI-4.⁸⁾ The microspacecraft was launched on June 19, 2014 and the MIPS was operated successfully in space on October 28, 2014 for the first time in the world. The neutralizer of the MIPS is based on a low-power microwave neutralizer for the 150-mAclass ion beam exhausted from an ion thruster,⁹⁻¹¹⁾ and employs the same frequency of 4.2 GHz and ring-shaped permanent magnets, but a different type of microwave antenna is used because of the small size of the MIPS neutralizer.¹²⁾

Although the MIPS has already been operated in space, the mechanism of electron
extraction from its neutralizer is still unclear and needs to be elucidated for a better performance.
Owing to its small size, the neutralizer operates using an identical discharge chamber, the same

45 microwave power, and a half gas flow rate compared with the ion source, which indicates that the MIPS neutralizer consumes resources (space, power, and propellant) more significantly than 46 conventional ion propulsion systems. One of the reasons for its poor performance is considered 47 to be the magnetic confinement of electrons inside the plasma source. Magnetic confinement is 48 49 necessary for good plasma production to reduce the loss of plasma toward the chamber wall. 50 The confinement, however, leads to a negative effect on electron extraction. Hence, it is 51 important to investigate the process through which electrons are extracted from the plasma source with applied magnetic fields. 52

In order to elucidate the extraction mechanism for a better performance of the 53 neutralizer, numerical simulations could be a powerful tool to compensate for the lack of 54 55 information obtained from experiments. Hence, we have developed a three-dimensional numerical model, which consists of a particle-in-cell simulation with a Monte Carlo collision 56 algorithm (PIC-MCC) for the kinetics of charged particles,¹³⁾ a finite-difference time-domain 57 (FDTD) algorithm for the electromagnetic fields of microwaves,¹⁴⁾ and a finite element analysis 58 59 for the magnetostatic fields of permanent magnets. The numerical analysis was performed for the plasma source,¹⁵⁾ and now is being used for the study on electron extraction. Numerical 60 results were compared with experimental data, in which the current density distribution on the 61 discharge chamber wall was obtained, and showed a reasonable agreement.^{16,17} 62

In the present work, to investigate the mechanisms of electron extraction from the
 micro-ECR neutralizer of the MIPS, we have conducted three-dimensional PIC-MCC

65 simulations and focused mainly on the electron trajectories extracted from the plasma source to the outside (vacuum) through orifices. This paper is an extended version of our conference 66 proceedings paper.¹⁸⁾ In the next section, we briefly describe our numerical model,¹⁵⁾ which 67 was extended to three dimensions from two axisymmetric dimensions for a micro-RF ion 68 thruster,¹⁹⁾ and a miniature inductively coupled plasma source.^{20,21)} In Sect. 3, we present the 69 results of macroscopic parameters and electron trajectories, which show that the self-generated 70 71 electrostatic field inside the plasma source is the most important factor and the $E \times B$ drift velocity at the orifice edges is one of the possible mechanisms to extract electrons, which is 72 newly added in the present paper. Finally, conclusions are drawn of this paper in Sect. 4. 73

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75 2. Numerical model

The three-dimensional PIC-MCC model described in our previous paper was employed under 76 the following assumptions.¹⁵⁾ (i) Only singly ionized xenon and electrons are treated as particles. 77 The reactions taken into account are elastic scattering, excitation, and ionization for electrons,²²⁻ 78 ²⁴⁾ and elastic scattering and charge exchange for ions,²⁵⁾ where the null-collision method is 79 employed to reduce the calculation time.²⁶⁾ The motion of excited-state atoms and Coulomb 80 81 collisions are not taken into account. Neutral particles are assumed to be spatially uniform 82 throughout the simulation and have a Maxwellian velocity distribution at a gas temperature of 83 300 K. (ii) The magnetic fields of microwaves are neglected compared with the magnetostatic fields of the permanent magnets. (iii) The effect of plasma current is not taken into account 84

owing to the low power of microwaves in this study.²⁷⁾

The numerical simulations were carried out as shown in Fig. 1. First, we set the initial 86 conditions and then solve Maxwell's equations by FDTD for the electromagnetic fields of 87 microwaves with a time increment $\Delta t_{\rm EM} = 2.98 \times 10^{-13}$ s (1/800 of a microwave cycle for 4.2 88 89 GHz) until we obtain a steady-state solution without plasma. We use the amplitude of the 90 electric fields of microwaves, E_0 , in the steady state for the PIC-MCC calculations as described 91 below. Second, electrostatic PIC-MCC calculations are conducted with a time step $\Delta t_e =$ 5.95×10^{-12} s (1/40 of a microwave cycle) using the electrostatic field **E**_{ES} of the plasma, the 92 time-varying electric field of microwaves $E_{\rm EM} = E_0 \cos(\omega t)$, and the magnetostatic fields $B_{\rm st}$ 93 generated by the permanent magnets, where ω is the angular frequency of microwaves and B_{st} 94 is determined using ANSYS EmagTM software. Here, in order to speed up the simulation, the 95 motion of ions is updated with a time step $\Delta t_i = 2.38 \times 10^{-10}$ s (one microwave cycle) by 96 97 neglecting $E_{\rm EM}$ and using the time-averaged $E_{\rm ES}$ over one microwave cycle because the 98 frequency of 4.2 GHz is much higher than the ion plasma frequency. In the simulation, the power absorbed in the plasma P_{abs} is used as an input parameter, where P_{abs} is obtained by 99 100 calculating the change in the kinetic energy of electrons and ions before and after the calculation of the equation of motion.²⁸⁾ Last, we rescale the amplitude E_0 to yield the specified power 101 102 absorbed in the plasma P_0 and iterate the above procedure until the steady-state solution is 103 obtained.

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Figure 2 shows the computational domain and dimensions for electron extraction in

105 the present study. The Cartesian coordinate system is employed and its origin is set at the center 106 of the ring-shaped antenna on the interface between the metal wall and the plasma in the z107 direction. The lengths in the x, y, and z directions are 20, 20, and 10 mm, respectively, including 108 the region for the investigation of electron extraction. The structure of the antenna and ringshaped magnets are the same as those employed in our previous paper,¹⁵⁾ in which the 109 dimensions are indicated in detail. We place a 0.6-mm-thick orifice plate at z = 4.0 mm, where 110 111 four orifices with a diameter of 2.2 mm are formed and their centers are located on the circle with a 5.0 mm radius of the x-y origin at an angular degree of 45 with respect to the x/y-axis. 112 113 The grid spacing is set at 0.2 mm at regular intervals. For the plasma parameter range calculated 114 in the present study, the grid spacing (Δx , Δy , and Δz) is small enough to satisfy the following condition: the Debye length λ_D is roughly larger than $\Delta x/3$, $\Delta y/3$, and $\Delta z/3$.²⁹⁾ As boundary 115 116 conditions, the potential on the entire metal area is set at zero and we set 20 V at z = 10 mm for 117 electron extraction. All electrons and ions disappear at the walls, antenna, and other boundaries, 118 where no reflection and charge accumulation are assumed.

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120 **3. Results and discussion**

121 A xenon plasma discharge was calculated for the microwave discharge neutralizer under the 122 base case condition; namely, the xenon gas pressure is 1 mTorr, the microwave frequency is 123 4.2 GHz, and the absorbed power is 0.3 W. The initial densities of both electrons and ions are 124 set at 1.0×10^{16} m⁻³ and are distributed uniformly in the simulation area. The initial electron and 125 ion temperatures are 2.0 and 0.05 eV, respectively.

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127 **3.1.** Macroscopic parameters

The macroscopic parameters, such as electron density and electron temperature, were 128 129 determined by averaging over 50000 microwave cycles (11.9 µs) after the steady state was reached. The peak plasma density is located in the ECR layer on the right side of the antenna, 130 where the maximum electron density is 1.6×10^{17} m⁻³, and their distributions spread along the 131 132 magnetic field lines, producing the ring-shaped profile of plasma density. Such a distribution 133 was also confirmed in the experiment. This result indicates that the plasma is well confined 134 because of the mirror magnetic fields. The distributions of electron temperature and plasma 135 potential are almost the same as the distribution of plasma density, where the peak electron temperature and potential obtained are 16 eV and 22 V, respectively. The details of the other 136 results are described in our previous paper.¹⁵⁾ 137

To investigate the mechanism of electron extraction through the orifices of the neutralizer, we have obtained the time-averaged electron current streamlines, as shown in Fig. 3, where the distributions of electron current density are also plotted as cross-sectional views. The figure clearly indicates the grad-*B* and curvature drift of electrons due to the magnetostatic field of the permanent magnets. Some electrons seem to flow back into the plasma source from the outside. Although the circulation of the electrons can be explained by the drift motion, the mechanism of electron motion in the *z* direction cannot be fully understood unless only the 145 time-averaged electron motion is focused on.

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- 147 3.2. Force exerted on a single electron

148 As described in Sect. 2, the motion of electrons are attributed to the sum of the electrostatic 149 electric field $E_{\rm ES}$, the microwave electromagnetic field $E_{\rm EM}$, and the magnetostatic field of the 150 permanent magnets B_{st} . Electron-neutral collisions also affect the electron motion. However, 151 their effect would be relatively small because of few collisions at a low pressure of 1 mTorr in 152 this work. To determine which effect plays a dominant role in extracting electrons from the confined plasma source through the orifice, we have conducted several simulations with 153 154 deletion of a portion of electromagnetic fields artificially after the steady-state solution is 155 obtained and tracked the motion of electrons. The results are summarized as follows. The 156 magnetostatic field B_{st} causes only the mirror confinement and grad-B and curvature drift, so that the electron trajectory only shows a circulation, similar to the electron current streamlines, 157 158 as shown in Fig. 3. Although the addition of $E_{\rm EM}$ resulted in only a slight change, the addition 159 of $E_{\rm ES}$ clearly has a strong effect on the electron trajectory inside the plasma source and 160 electrons are extracted from the orifice. Electrons are not extracted unless the effect of E_{ES} is taken into account in the calculations.^{16,17)} 161

162 Electrons have to overcome the potential barrier as well as escape from the magnetic 163 confinement in order to be extracted through the orifice. Since the force due to E_{ES} exerts on 164 electrons in the opposite direction of extraction, the distribution of E_{ES} does not show a clear

165	reason for extraction from the bulk plasma into the vacuum through the orifice, although $E_{\rm ES}$ is
166	required for electron extraction. An electron moves along the magnetic field line and travels
167	back and forth as a result of its confinement due to the mirror magnetic fields, as shown in Fig.
168	2(d). The electron trajectory can move from one of the magnetic field lines to another line when
169	the electron is reflected by the potential barrier in the sheath. If the trajectory was going outward
170	gradually, the electron could be extracted through one of the orifices. ^{16,17)}

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172 3.3. Cross-field motion

173 Since cross-field motion of grad-B and curvature drift only results in the circulation of electrons 174 along the ring-shaped antenna, as shown in Fig 3, one of possible mechanisms of cross-field 175 motion for electron extraction is the $E \times B$ drift motion. Figure 4 shows the two-dimensional 176 distribution of the time-averaged $E \times B$ drift velocity in the z direction at the orifice plate (z = 177 4.0 mm), which is obtained from the electric and magnetic fields at the grid points. As clearly 178 seen in the figure, the positive drift velocity is obtained on the clockwise side of the orifice 179 while the negative drift velocity is seen on the counterclockwise side. Since two ring-shaped 180 permanent magnets are employed, the axisymmetric magnetic field is generated with respect to 181 the x-y origin. The direction of the time-averaged electric field inside the orifice is from the 182 center to the edge of the orifice. These magnetic and electric fields produce the drift velocity 183 component at the edge of the orifice.

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To investigate the $E \times B$ drift effect, 1000 electrons are sampled at random and then

185 their trajectories are traced for a time span of 2000 microwave cycles (476 ns). Figure 5 shows 186 a scatter diagram of electrons at the orifice plate (z = 4.0 mm), in which the positions of the 187 electrons having a drift velocity in the outgoing direction from the plasma source to the vacuum 188 are plotted in red while those of electrons having a drift velocity in the incoming direction from 189 the vacuum to the plasma source are plotted in blue. It seems likely that the tendency of electron 190 distribution inside each orifice is quite similar to the time-averaged $E \times B$ drift velocity in the z 191 direction, as shown in Fig. 4. A typical trajectory of a single electron extracted from one of the 192 orifices together with vectors of $E \times B$ drift velocity at some points is shown in Fig. 6, in which 193 the plane is set in such a way that it always passes through both the positions of the electron 194 and the z-axis during the electron tracking. Although the electron does not directly follow the 195 direction of $E \times B$ drift velocity, at least its projected direction is consistent with the electron 196 motion.

197 Figure 7(a) shows the number of outgoing and incoming electrons passing through 198 different regions inside the orifices; the regions are defined in Fig. 7(b). Each region is divided 199 by lines passing through the x-y origin at regular intervals of five angular degrees. While the 200 number of incoming electrons are larger than that of outgoing electrons at 50 angular degrees 201 or larger (on the counterclockwise side of the orifice), the number of outgoing electrons are 202 larger than that of incoming electrons at less than 50 angular degrees (on the clockwise side). 203 This tendency is consistent with the distribution of the time-averaged $E \times B$ drift velocity in the z direction, as shown in Fig. 4. The plasma density inside the plasma source is much higher 204

than that in the vacuum area; thus, the number of outgoing electrons through the orifice region below 40 angular degrees are larger than that of incoming electrons through the orifice region over 50 angular degrees, although both regions have the same area and the same magnitude of force is exerted. However, there are almost no force that induces the $E \times B$ drift in the central area of the orifice, where the largest number of electrons is extracted from the plasma source to the vacuum. This extraction mechanism cannot be explained by the $E \times B$ drift motion only and is still left for future work.

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213 **4. Conclusions**

214 We have conducted three-dimensional PIC-MCC simulations to investigate the mechanisms of 215 electron extraction for a micro-ECR neutralizer. The simulations have shown that electrons are not extracted unless the effect of E_{ES} is taken into account; thus, the electron extraction is 216 217 mainly attributed to the self-generated electrostatic field inside the plasma source, even though 218 $E_{\rm ES}$ gives the opposite force of electron extraction from the bulk plasma toward the orifice plate. 219 If the electrons are trapped in the magnetic field passing close to the orifice, such electrons can 220 move to just before the orifice because of magnetic confinement. Although the extraction 221 mechanism at the central area of the orifice is still not clear, the $E \times B$ drift provides the 222 mechanism by which electrons are extracted from the plasma source to the outside at the orifice 223 edge.

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274 List of Figure Captions

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Fig. 1. Flow chart of the three-dimensional particle model. First, initial conditions are set and Maxwell's equations are solved by FDTD for the electromagnetic fields of 4.2 GHz microwaves to obtain a steady-state solution without plasma. Second, electrostatic PIC-MCC calculations are performed using the electrostatic field E_{ES} , the time-varying electric field of microwaves E_{EM} , and the magnetostatic fields of permanent magnets B_{st} , which is determined using ANSYS EmagTM software. In the simulation, the power absorbed in the plasma P_0 is used as an input parameter.

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Fig. 2. (Color online) Computational area and dimensions for calculations of the micro-ECR neutralizer, including the vacuum region for electron extraction: (a) *x-y* plane (z = 1.0 mm) at the antenna, (b) *z-x/y* plane (y/x = 0.0 mm), and (c) *x-y* plane (z = 4.0 mm) at the orifice plate. (d) Contour plots at the *z*–*y* plane (x = 0.0 mm) of the strength of the magnetic field of the ringshaped permanent magnets and the magnetic field lines in black, together with the thick lines in red representing the resonant magnetic field of 0.15 T for 4.2 GHz microwaves.

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Fig. 3. (Color online) Cross-sectional views of the time-averaged electron current density and a few examples of its streamlines under the base case condition, where the xenon gas pressure is 1 mTorr, the microwave frequency is 4.2 GHz, and the absorbed power is 0.3 W. Fig. 4. (Color online) Two-dimensional distribution of the time-averaged $E \times B$ drift velocity in the *z* direction at the orifice plate (*z* = 4.0 mm), together with circles in black representing the boundaries of the ring-shaped permanent magnets and the four orifices. Note that the contours in red represent the current density in the positive *z* direction (from the plasma source to the vacuum).

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Fig. 5. (Color online) Scatter diagram of the positions for outgoing (red dots) and incoming (blue dots) electrons at the orifice plate (z = 4.0 mm), together with circles in black representing the boundaries of the ring-shaped permanent magnets and the four orifices. Here, 1000 electrons are sampled at random upstream of the upper left orifice, and their trajectories are traced for a time span of 2000 microwave cycles.

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Fig. 6. (Color online) Typical trajectory of a single electron extracted through one of the orifices together with vectors of the $E \times B$ drift velocity at some points, where the plane is set in such a way that the plane always passes through both the positions of the electron and the *z*-axis during the electron tracking.

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Fig. 7. (Color online) (a) Number of outgoing and incoming electrons passing through different regions inside the orifices at z = 4.0 mm and (b) the definition of the regions.



Fig. 1





- 324 Fig. 3





Fig. 4







Fig. 5







Fig. 7