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CORRECTIONS TO "DIRICHLET PROBLEM FOR MINIMAL SURFACE EQUATIONS IN A RIEMANNIAN MANIFOLD I"

By

RYOSUKE ICHIDA

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The above paper ([3]) contains errors. We correct them as follows:

p. 127, line 11 of Introduction, "$\sum_f=\{S(u);\ u\in F\}$" should read "and we set $\sum_f=\{S(u);\ u\in F\}$".

p. 127, line 7 from bottom, "Supposing that..., in Section" should read "In Section".

p. 129, line 15, the term $-(\sum_{k=1}^{n}\rho_k p^k)/2\rho$ in $B(x, p)$ should be $-(\|p\|^2/2+1/\rho)\cdot(\sum_{k=1}^{n}\rho_k p^k)$.

p. 131, line 6 from bottom, "non-zero vector" should read "a non-zero vector".

p. 131, line 2 from bottom, $\{\sum_{i,j,k=1}^{n}(g^{ij}-\sigma^i\sigma^j)\Gamma_{ij}^k\sigma_k\}$ should be

$$\{\sum_{i,j,k=1}^{n}(g^{ij}-\sigma^i\sigma^j)\Gamma_{ij}^k\sigma_k-(\sum_{k=1}^{n}\rho_k\sigma^k)/2\rho\}.$$

p. 132, line 14, $\|p\|\geqq 2c_1$ should read $p-p_0=\|p-p_0\|v$ and $\|p\|\geqq 2c_1$, $|\|p-p_0\|-\|p\||\leqq c_1$.

p. 133, line 3, $\mathscr{C}_0(\bar{x}, v)$ should be

$$\begin{aligned}\mathscr{C}_0(\bar{x}, v)&=\left\{\sum_{i,j=1}^{n-1}g^{ij}(\bar{x})\Gamma_{ij}^n(\bar{x})-\frac{1}{2}\frac{\partial\log\rho}{\partial n}(\bar{x})\right\}\Big/\left(\sum_{k=1}^{n-1}g^{kk}(\bar{x})\right)\\&=\left\{(n-1)H(\bar{x})-\frac{1}{2}\frac{\partial\log\rho}{\partial n}(\bar{x})\right\}\Big/\left(\sum_{k=1}^{n-1}g^{kk}(\bar{x})\right)\end{aligned}$$

where $\dfrac{\partial}{\partial n}$ denotes the inward unit normal vector to the boundary ∂M.

p. 133, line 6, $H\geqq 0$ should read $2(n-1)H\geqq\dfrac{\partial\log\rho}{\partial n}$.

p. 133, line 14, $(0<r<d_1)$ should read $(0<r<r_1)$.

p. 134, lines 1–2, "Assume that...everywhere" should read as follows: "Assume that the mean curvature H (with respect to the inward direction) of ∂M satisfies $2(n-1)H\geqq\dfrac{\partial\log\rho}{\partial n}$ on ∂M".

p. 134, line 7, $\sup_{\partial M} |f| = c_0$ should read $\sup_{M} |f| = c_0$.

p. 134, line 7, $m_1 = 2c_0$ should read $m_1 = 2c_0 + 1$.

p. 134, line 8, (3.13) should read (3.14).

p. 134, line 11, $f + 2c_0$ should read $f + m_1$.

p. 134, line 7 from bottom, the term $-a^2(D\rho \cdot p)/2\rho$ in $B(x, p)$ should be $-(|p|^2/2 + a^2/\rho)(D\rho \cdot p)$.

p. 135, line 2, $\mathscr{C}_0(x, \sigma)$ should be $\mathscr{C}_0(x, \sigma) = -\{(Da \cdot \sigma)/a + (D\rho \cdot \sigma)/2(n-1)\rho\}$.

p. 136, line 7, $H \geqq 0$ should read $2(n-1)H \geqq \dfrac{\partial \log \rho}{\partial n}$.

p. 136, line 14 from bottom, "assume that...everywhere" should read as follows: "assume that the mean curvature H (with respect to the inward direction) of $\partial\Omega$ satisfies $2(n-1)H \geqq \dfrac{\partial \log \rho}{\partial n}$ on $\partial\Omega$."

p. 137, line 12, the term $-a^2(D\rho \cdot Du)/2\rho$ in equation (5.4) should be $-(|Du|^2/2 + a^2/\rho)(D\rho \cdot Du)$.

p. 137, lines 17–18, "Assume that...everywhere" should read as follows: "Assume that the mean curvature H (with respect to the inward direction) of $\partial\Omega$ satisfies $2(n-1)H \geqq \dfrac{\partial \log \rho}{\partial n}$ on $\partial\Omega$".

Finally we correct the errors in the papers [1], [2] as follows:

p. 171, line 6 from bottom and p. 172, line 3 of [1], $(\Gamma^\alpha_{ij} + \Gamma^\alpha_{in+1} u_j)$ should read $(\Gamma^\alpha_{ij} + \Gamma^\alpha_{in+1} u_j + \Gamma^\alpha_{jn+1} u_i + \Gamma^\alpha_{n+1n+1} u_i u_j)$.

p. 174, lines 12, 23 of [2], $(\Gamma^k_{ij} + \Gamma^k_{in+1} u_j)$ should read $(\Gamma^k_{ij} + \Gamma^k_{in+1} u_j + \Gamma^k_{jn+1} u_i)$.

p. 180, lines 2, 11 of [2], $(\Gamma^\alpha_{ij} + \Gamma^\alpha_{in+1} u_j)$ should read $(\Gamma^\alpha_{ij} + \Gamma^\alpha_{in+1} u_j + \Gamma^\alpha_{jn+1} u_i + \Gamma^\alpha_{n+1n+1} u_i u_j)$.

References

[1] R. Ichida: *On hypersurfaces in a homogeneous Riemannian manifold.* The Yokohama Math. J., **25**, 169–182 (1977).

[2] R. Ichida: *On uniqueness for existence of minimal hypersurfaces a given boundary in a Riemannian manifold.* The Yokohama Math. J., **26**, 169–188 (1978).

[3] R. Ichida: *Dirichlet problem for minimal surface equations in a Riemannian manifold.* The Yokohama Math. J., **27**, 127–139 (1979).

Department of Mathematics
Yokohama City University
22–2 Seto, Kanazawa-ku
Yokohama, 236 Japan